Algebra 2

6.3: Logarithms (Day 3 Worksheet)

Note the "NC" and "C" indications. When using a calculator, round final answers to three decimals.

1. Solve each equation by getting a common base. NC

a.
$$3^{2(x-3)} = 27^{8x}$$

b.
$$27^x = \left(\frac{1}{81}\right)^2$$

c.
$$\left(\frac{4}{9}\right)^x = \frac{81}{16}$$

d.
$$16 = \left(\frac{1}{8}\right)^x$$

e.
$$3^{2x+1} = 81^x$$

$$\mathbf{f.} \ \frac{1}{4^x} = 64^{x+1}$$

2. Solve each equation for x using an appropriate strategy. Show all work. NC

a.
$$6\log(x+2) = 12$$

b.
$$3 \cdot 6^x = 108$$

c.
$$32^{x-1} = \left(\frac{1}{2}\right)^{6x}$$

d.
$$\log_2(3x+1) = \log_3 243$$
 e. $3\log_5 125 = 7x+2$

e.
$$3\log_5 125 = 7x + 2$$

f.
$$4^{3x} + \log_9 1 = \frac{1}{128}$$

3. Find at least two *integer* ordered pairs you could use to graph the functions below.

$y = \log_2 x$			
X			
у			
$y = \log_4 x$			
X			
ν			

$y = \log_3 x$			
X			
У			
$y = \log_5 x$			
х			
λ			

4. Max solved the equation, $5^{x+3} = 25^{x-2}$, but made an error. His work is shown below. Circle the step in which the error appears, then correctly solve the problem in the space below.

$$25^{x-2} = 5^{x+3}$$

$$(5^{2})^{x-2} = 5^{x+3}$$

$$5^{2x-2} = 5^{x+3}$$

$$2x-2 = x+3$$

$$x = 5$$

5. Scott's parents bought him a really nice car when he was a senior (lucky duck!). Now a beginning software engineer, Scott wants to sell his car and commute via bicycle (health benefits!). He made \$25,000 from the sale and wants to invest it in a low-risk account that is compounded monthly. The interest rate he'll get is 6% (lucky duck!). If Scott just turned 23 when he invests the money, what will be his age when the account doubles in value? Show each step algebraically without using a calculator until your final step. Justify your final answer.

6. The decibel (dB) scale is based on the formula below. A typical vacuum cleaner registers at 80 dB, and a typical rock concert registers at 120 dB. How many times more intense in sound is a typical rock concert compared to a typical vacuum cleaner? *NC*

 $N_{dB} = 10 \log \left(\frac{I}{I_0} \right)$; N_{dB} is the change in decibel level; $\frac{I}{I_0}$ is the intensity ratio of the two sounds

7. Use the information from question (6). If human breathing registers at 10 dB, how many times more intense in sound is a rock concert compared to human breathing? *NC*