

Name: _____

8.1 Radicals & Pythagorean & Converse

Date: _____ Period: _____

Key

1-10 Simply the expressions by leaving your answer in reduced radical form.

$$1. \frac{\sqrt{24}}{\sqrt{4 \cdot 6}} = 2\sqrt{6}$$

$$2. -\sqrt{72} = -(\sqrt{36 \cdot 2}) = -6\sqrt{2}$$

$$3. \frac{\sqrt{6 \cdot 8}}{\sqrt{16 \cdot 3}} = \frac{\sqrt{48}}{4\sqrt{3}} = \frac{4\sqrt{3}}{4\sqrt{3}} = 1$$

$$4. -4\sqrt{8} + 2\sqrt{8} = -2\sqrt{8} = -2(2\sqrt{2}) = -4\sqrt{2}$$

$$5. 2\sqrt{12} = 2\sqrt{4 \cdot 3} = 2 \cdot 2\sqrt{3} = 4\sqrt{3}$$

$$6. \frac{3}{\sqrt{6}} = \frac{3\sqrt{6}}{6} = \frac{\sqrt{6}}{2}$$

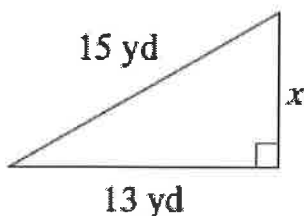
$$7. \frac{8}{\sqrt{12}} = \frac{8\sqrt{12}}{12} = \frac{2(\sqrt{4 \cdot 3})}{3} = \frac{2 \cdot 2\sqrt{3}}{3} = \frac{4\sqrt{3}}{3}$$

$$8. \frac{\sqrt{4}}{4\sqrt{5}} \cdot \frac{\sqrt{5}}{\sqrt{5}} = \frac{\sqrt{20}}{20} = \frac{\sqrt{4 \cdot 5}}{20} = \frac{2\sqrt{5}}{20} = \frac{\sqrt{5}}{10}$$

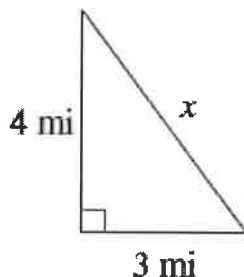
$$9. \sqrt{4} - \sqrt{16} + \sqrt{2} - 6\sqrt{2} = 2 - 4 + \sqrt{2} - 6\sqrt{2} = -2 - 5\sqrt{2}$$

$$10. 5\sqrt{7} + \sqrt{3} - 8\sqrt{7} = -3\sqrt{7} + \sqrt{3}$$

11. Find the missing side of each triangle. Leave your answer in reduced radical form.



$$15^2 = 13^2 + x^2 \\ \sqrt{15^2 - 13^2} = x \\ \sqrt{56} = x \\ \sqrt{4 \cdot 14} = x \\ 2\sqrt{14} = x$$

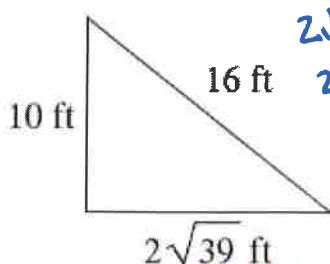


$$4^2 + 3^2 = x^2 \\ \sqrt{25} = x \\ 5 = x$$

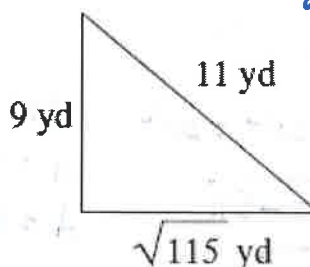


$$16^2 = 8^2 + x^2 \\ \sqrt{16^2 - 8^2} = x \\ \sqrt{192} = x \\ \sqrt{64 \cdot 3} = x = 8\sqrt{3}$$

12. State if each triangle is a right triangle. Then find the perimeter of the triangle in reduced radical form.



$$2\sqrt{39} + 10 + 16 = 26 + 2\sqrt{39} \\ 16^2 = 10^2 + (2\sqrt{39})^2 \\ 256 = 100 + 4 \cdot 39 = 256 \quad \text{yes}$$



$$9^2 + 11^2 = 112 \neq 115 \\ 9 + 11 + \sqrt{115} = 20 + \sqrt{115} \quad \text{no}$$

13. State if the three side lengths form a right triangle.

6, $2\sqrt{22}$, 17
 $6^2 + (2\sqrt{22})^2 = 17^2$
 $36 + 4(22) = 289$
 $124 \neq 289$
 NO

4.8, 28.6, 29
 $4.8^2 + 28.6^2 = 29^2$
 $23.04 + 817.96 = 841$
 $841 = 841$
 yes

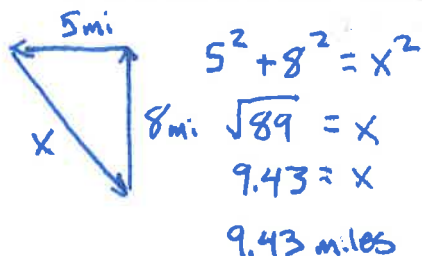
Questions 14-17 round your answers to the nearest hundredth if necessary.

14. Tina built a ^{triangular} sign with side lengths of 73 inches, 55 inches, and 4 feet. Is the sign a right triangle? Why or why not?

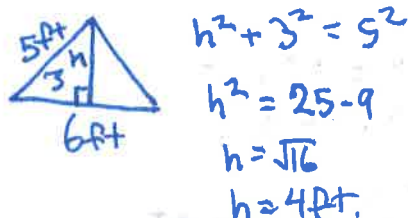
$73^2 = 55^2 + 48^2$ yes because the Pythagorean Theorem holds true for the 3 sides
 $5329 = 3025 + 2304$
 $5329 = 5329$

~~no~~ $(6.0\overline{6})^2 = (4.5\overline{8})^2 + 4^2 \approx 37.01$

15. Two joggers run 8 miles north and then 5 miles west. What is the shortest distance they must travel to return to their starting point?

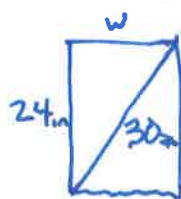


16. Oscar's dog house is shaped like a tent. The slanted sides are both 5 feet long and the bottom of the house is 6 feet across. What is the height of his dog house, in feet, at its tallest point?



The tallest point is 4 feet.

17. A suitcase measures 24 inches long and the diagonal is 30 inches long. How much material is needed to cover one side of the suitcase?



$24^2 + w^2 = 30^2$
 $w = \sqrt{900 - 576}$
 $w = \sqrt{324}$
 $w = 18$ in

$A = lw$
 $A = 24 \cdot 18$
 $A = 432$ in²

432 in² of materials is needed to cover one side